

Vol. 36, No. 01 (Especial), pp. 26-37/Marzo 2023

Simulation of a continuous fluidised bed dryer for paddy[†]

Simulación de un secador continuo de lecho fluidizado para arroz

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(recibido/received: 15-abril-2022; aceptado/accepted: 26-agosto-2022)

ABSTRACT

A model for simulating the drying of paddy (*Oryza sativa* L.) in a continuous fluidised bed dryer was employed. Equipment and material models were applied to describe the process. The equipment model was based on the differential equations obtained by applying mass and energy balances to each element of the dryer. In the case of the material model, mass and heat transfer rates in a single isolated particle were considered. Simulation results were verified by comparison with experimental data from the literature. There was a very good agreement between experimental data and simulation. The effects of gas temperature and velocity, particle diameter, dry solid flow, and solid temperature on the drying process were studied. It was found that the changes in gas velocity, dry solids flow, and solid temperature had essentially no effect on the drying process.

Keywords: Paddy; Fluidised bed dryer; Plug-flow; Simulation

RESUMEN

Se empleó un modelo para simular el secado de arroz (*Oryza sativa* L.) en un secador continuo de lecho fluidizado. Se aplicaron modelos de equipo y material. El modelo de equipo se basó en las ecuaciones diferenciales obtenidas al aplicar balances de masa y energía a cada elemento del secador. En el caso del modelo de material, se consideraron velocidades de transferencia de masa y calor en una partícula aislada. Los resultados de la simulación fueron verificados por comparación con datos experimentales de la literatura. Hubo una muy buena concordancia entre los datos experimentales y la simulación. Se estudiaron los efectos de la temperatura y velocidad del gas, diámetro de partícula, flujo de solidos secos y temperatura del solido en el proceso de secado. Se encontró que los cambios en la velocidad del gas, flujo de solidos secos y temperatura del sólido esencialmente no tuvieron efecto en el proceso de secado.

Palabra claves: Arroz; secador de lecho fluidizado; Flujo pistón; Simulación

† In honour and loving memory of *Prof. em. Dr.-Ing. habil. Luis Moreno* (1942-2022).

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1. INTRODUCTION

Paddy (*Oryza sativa* L.) is the predominant staple food throughout the world, feeding more than half of the world's population. Moisture content is one of the most important factors influencing the quality of paddy during storage and it remains at a high level during the harvest 20-30 % (dry basis) and must be reduced with an appropriate drying process. The drying characteristics of paddy have been studied by many researchers and various models for the prediction of drying rate have been developed (Hacıhafızoğlu *et al.*, 2008).

Fluidised bed drying is the most used drying method to preserve foods and agricultural products and among several methods for drying moist granular materials, fluidised bed drying has been one of the most successful techniques and widely used during postharvest processing of agricultural grain (Mujumdar, 2014). In this drying method, solid moist particles are suspended in a hot air stream and a high rate of heat and mass transfer takes place between the grain and gas.

Numerous types of fluidised bed dryers have been developed in various industries, among which, well-mixed, plug-flow, vibrated, agitated and centrifugal fluidised bed dryers are the most important ones. Despite this variety, the well-mixed and plug-flow fluidised bed dryers are the most common types, which can cover other above-mentioned types of dryers.

Most of the existing models of plug-flow fluidised bed dryers are based on knowledge of the interaction between the solid and gas phases. For instance, Gagnon *et al.* (2021) developed a dynamic model with lumped parameters of a continuous horizontal fluidised bed dryer equipped with a screw conveyor. The dynamic model includes a two-phase tanks-in-series configuration, thus considering gas bypasses (bubbles) and product axial mixing. Simulation results for calcium carbonate granules are consistent with theory. Verma and Paliwal (2020) reported a mathematical model for a continuous plug flow fluidised bed dryer. The model equations are solved by an iterative scheme with the implicit method of discretisation along with a desired convergence.

Khanali *et al.* (2013) reported a model for a plug-flow fluidised bed dryer under steady-state conditions based on partial differential equations. A very satisfactory agreement between the theoretical and experimental data was achieved. Further, Bizmark *et al.* (2010) reported a sequential method to model a continuous plug-flow fluidised bed dryer, which is based on dividing the dryer into sections in series with ideal mixing for both solid and gas phases in each section. It was shown that the model fitted the experimental data satisfactorily. Daud (2007) has used the steady-state cross-flow model for estimating the profiles for solids and air moisture contents and temperatures in a continuous fluidised bed dryer. These profiles were shown to be dependent on the gas-solid flow ratio.

Izadifar and Mowla (2003) developed a mathematical model to simulate the drying of moist paddy rice in a cross-flow continuous fluidised bed dryer, applying momentum, mass, and energy balances to each element of the dryer. Also, the non-ideal flow of solids in plug-flow fluidised dryers has been modelled as several continuous back-mixed fluidised bed dryers connected in several ways (Wanjari *et al.*, 2006; Baker *et al.*, 2010). The problem with this type of model is the difficulty of estimating enough completely mixed dryers for any dryer a priori. It could only be determined by an analysis of pilot-plant data (Daud, 2008).

Building on the results of an earlier study (Picado and Martínez, 2012), the present work was aimed to study the simulation of a continuous fluidised bed dryer for paddy (*Oryza sativa* L.). This was done by incorporating a material model for a single wet grain, amenable to be solved analytically, in an incremental equipment model assuming plug-flow of the solids with gas cross-flow. The validity of the model was tested by comparison of model predictions with experimental data from the literature.

2. DESCRIPTION OF THE MODEL

A schematic description of a continuous plug-flow fluidised bed dryer is shown in Fig. 1. Paddy grains enter the dryer by a helical feeder and are fluidised smoothly by the upward flow of gas, normally air coming from the bottom of the bed through a gas distributor. An effective mixing of the paddy grains takes place and a homogeneous material at a vertical cross-section of the dryer is usually obtained. Due to fluidisation and the slope of the dryer, paddy grains move forward along the dryer and a partially dry product exits from the end.

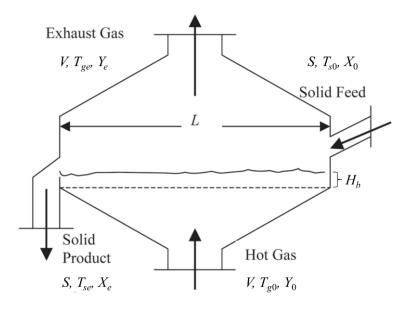


Fig. 1 A plug-flow fluidised bed dryer.

The details of the model have been presented elsewhere (Picado and Martínez, 2012) and only the essentials are outlined here. The following assumptions are introduced to simplify the complex characteristics of the process in the dryer:

- Paddy is a spherical grain, isotropic, uniform in size and homogenous.
- The grain is perfectly well mixed in the vertical direction.
- Shrinkage of the grain during drying is negligible.
- Physical properties of the dry grain remain constant with time.
- The inlet distribution of the moisture content and temperature is uniform.
- Heat and mass transfer inside the grain takes place only in the radial direction.
- Moisture at the grain surface is in equilibrium with the gas humidity.
- The dryer is perfectly insulated.

2.1 Mass and energy balances

In the analysis of the dryer, it was assumed that the bed of particles was moving forward at a uniform velocity and that the dryer had been operating for long enough to ensure that steady-state conditions were reached. A moisture balance applied to the differential volume element shown in Fig. 2 yields:

$$F_s \frac{dX_b}{dz} = -a_s M G_g \tag{1}$$

where X is the solid moisture content on a dry basis, M is the molecular weight of the moisture, a_s is the specific evaporation area per unit bed volume, G_g is the molar evaporation flux, F is a mass flow per cross-section in the direction of the flow, and z is the distance along the bed from the solids inlet. The subscripts s and b denote solid and bed, respectively.

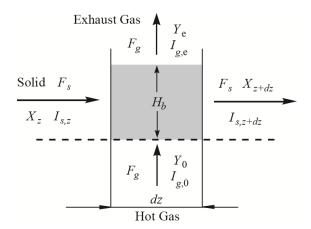


Fig. 2 Scheme of a differential dryer element.

Because all of the evaporated liquid goes to the gas, the following equation gives the change in gas humidity:

$$F_g dY = -F_s H_b \frac{dX_b}{dz} \tag{2}$$

where Y is the gas humidity on a dry basis and H_b is the bed height. The subscript g denotes gas. The bed height is calculated as

$$H_b = \frac{S}{\nu \rho_p (1 - \varepsilon_p)(1 - \varepsilon_b)B} \tag{3}$$

where S is the flow of dry solids, v is forward bed velocity, ρ is the density, ε is the porosity, and B is the dryer width. The subscript p denotes particle. Because heat losses in the dryer are neglected, the energy balance over the same differential volume element becomes:

$$dI_g = -H_b \frac{F_s}{F_a} \frac{dI_s}{dz} \tag{4}$$

where I is the enthalpy of the phases per unit mass on a dry basis. To integrate Eq. (1) to determine the changes in mean moisture content of the grain along the dryer, in addition inlet conditions, the evaporation flux must be provided. This flux depends on the temperature and moisture content at the surface of the particles. This information can be obtained by analysing what happens with a single particle moving along the dryer.

2.2 Drying of a single particle

The drying of a single wet particle into an inert gas is schematically described in Fig. 3. During the drying process, the moisture migrates from the centre of the solid particle towards the surface, where it

evaporates. Migration occurs due to the moisture gradient in the solid particle by several mechanisms: molecular diffusion (liquid and vapour), capillary flow, Knudsen diffusion, surface diffusion, or combinations of the foregoing mechanisms. Usually, all of these mechanisms are lumped into an effective liquid transport mechanism using Fick's law for mass flux, which seems to describe the experimental data fairly well (Mujumdar, 2014; Saravacos and Maroulis, 2001).

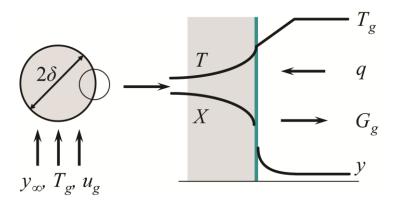


Fig. 3 Schematic of drying of a single particle into a gas.

Based on the assumptions outlined above, a set of space-averaged governing equations can be written for the particle. The longitudinal location of a particle in the dryer is related to the residence time (t) by the linear velocity of the bed (v). This allows one to track the changes in moisture content and temperature of particles as functions of distance along the bed (z). By introducing this change in variables, the diffusion equation for the spherical particle is

$$v\frac{\partial X}{\partial z} = D_{eff} \left(\frac{\partial^2 X}{\partial r^2} + \frac{2}{r} \frac{\partial X}{\partial r} \right) \tag{5}$$

where r is the radial coordinate and D_{eff} is the effective diffusion coefficient, which is estimated using an equation reported by Yamaguchi (1992).

If conduction is the only mechanism for heat transfer within the particle, the corresponding equation to describe temperature changes is the conduction equation:

$$v\frac{\partial T}{\partial z} = D_h \left(\frac{\partial^2 T}{\partial r^2} + \frac{2}{r} \frac{\partial T}{\partial r} \right) \tag{6}$$

where D_h is the thermal diffusivity of the wet grain and T is the temperature. Equations (5) and (6) represent a system of partial differential equations with the following inlet and boundary conditions:

At z = 0 and $0 \le r \le \delta$,

$$X = X_0\{r\};$$
 $T = T_0\{r\}$ (7)

At z > 0 and r = 0,

$$\frac{\partial X}{\partial r} = 0; \qquad \frac{\partial T}{\partial r} = 0 \tag{8}$$

At z > 0 and $r = \delta$,

$$-\rho_{p} D_{eff} \frac{\partial X}{\partial r} = M G_{g}; \quad -k_{eff} \frac{\partial T}{\partial r} = h(T - T_{g,\infty}) + \lambda G_{g}$$

$$(9)$$

where δ is the particle radius, k is the thermal conductivity of the wet solid, and λ is the latent heat of vaporisation. The subscripts 0, *eff*, and ∞ denote inlet, effective value, and gas bulk, respectively. Effective physical properties can be estimated by averaging the corresponding properties of the solid and moisture.

2.3 Mass and heat transfer rates

At the interphase, the evaporation flux is simply calculated as

$$G_{g} = k_{m} \left(y_{\delta} - y_{\infty} \right) \tag{10}$$

where k_m is the mass transfer coefficient, and y_{δ} and y_{∞} are the vapour molar fractions at the gas-wet solid interface and in the gas bulk, respectively. In a hygroscopic material, the vapour pressure at the surface will be lower than the saturated value. This is accounted for by introducing a sorption isotherm that relates the equilibrium vapour pressure at the solid surface to the saturated value. In the present study, an empirical equation reported by Pfost *et al.* (1976) is used to correlate experimental equilibrium data. This information is inserted into Eq. (10), where y_{δ} is given by the ratio between the partial pressure of water vapour and the total pressure.

The convective heat flux can be calculated as:

$$q = h \left(T_{g,\infty} - T_{\delta} \right) \tag{11}$$

where h is the heat transfer coefficient between the drying gas and particle and is estimated using a correlation reported by Yang (2003). The mass transfer coefficient can be calculated from the heat transfer coefficient by applying the Lewis relationship because the Prandtl and Schmidt numbers are almost equal for mixtures of water vapour and air (Mujumdar, 2014).

2.4 Implementation of the model

Equation (1) is a nonlinear ordinary differential equation that can be solved numerically using Euler's or any other standard method. Mass and heat transfer rates are required in the mass and energy balances along the dryer. The simultaneous solution of Eqs. (5) and (6), subjected to inlet and boundary conditions (7) through (9), provides the moisture content and temperature gradients in the particle as well as mass and heat transfer rates at the particle surface. By assuming constant transport coefficients as well as constant mass and heat transfer rates in each integration step of Eq. (1), Eqs. (5) and (6) can be solved analytically. The details of the analytical solutions and dimensionless variables as well as other parameters of the solutions can be found elsewhere (Picado and Martínez, 2012).

Because the conditions change along the dryer, the analytical solutions are applied to an interval dz, with inlet conditions and averaged transport coefficients corresponding to the outlet conditions of the previous step. As the integration of Eq. (1) proceeds, the procedure is repeated step by step. The outlet composition of the gas at each step dz is calculated using Eq. (2). Then the energy balance, Eq. (4), allows for the calculation of the exhaust gas enthalpy using the mean particle temperature to calculate the outlet enthalpy

of the wet solids. Because the gas enthalpy is a function of gas composition and temperature, the outlet gas temperature can be calculated from a nonlinear equation that relates gas temperature with the gas enthalpy. Integration proceeds in this way until the dryer exit is reached.

3. RESULTS AND DISCUSSION

3.1 Model validation

To investigate the validity of the model predictions, the theoretical results were compared with small-scale experimental data from the literature. The material under consideration was paddy from the Lucknow district, India. The experimental plug-flow fluidised bed dryer consisted of a chamber with a rectangular cross-section for the gas flow of $0.4~\text{m}\times0.07~\text{m}$ and a height of 0.07~m. To measure the moisture content, sampling was performed at three points along the dryer length at 0.12, 0.24~and~0.34~m from the solid inlet port. Details of the experimental procedure can be found elsewhere (Verma and Paliwal, 2022). The experimental data sets were either cited directly from tables or read (digitised) from experimental points on figures in Verma and Paliwal (2022). The basic physical properties of paddy used in the simulation are summarised in Table 1.

Table 1 Physical properties of paddy (Khanali et al., 2012; Khanali et al., 2013)

| Particle diameter (m) | 3.55×10^{-3} |
|---------------------------------------|-----------------------|
| Particle density (kg/m ³) | 1131 |
| Particle porosity | 0.56 |
| Particle sphericity | 0.40 |
| Specific heat (J/kg K) | 1110 |
| Thermal conductivity (W/m K) | 0.10 |

Figure 4 shows a comparison between the mean moisture content and mean solid temperature predicted by the mathematical model and experimental data for the same operating conditions. Both cases exhibited a very good agreement with the experimental data. As can be seen in Fig. 4, the predicted and experimental moisture content exhibited a smooth exponential decay curve over the whole length of the dryer, which characterises the drying in the falling rate period for hygroscopic materials.

Air drying of many foods and agricultural products, such as paddy, displays no constant rate period and the internal resistance to moisture transfer controls the drying process (Mujumdar, 2014). Further, similar axial profiles of moisture content for plug-flow fluidised bed drying employing different materials have been reported (Baker *et al.*, 2006; Wanjari *et al.*, 2006; Baker *et al.*, 2010; Khanali *et al.*, 2013).

The temperature of the solids progressively rises as they move from the feed point to the dyer exit. In the end stage of drying, the mathematical model overestimates the solid temperature of paddy. However, it is difficult to discern whether it is due to limitations of the model or uncertainties in the experimental data. Due to the complex flow pattern in the dryer, it is not always possible to obtain representative samples. Additionally, measuring the true particle temperature is a difficult task.

A series of simulations were also undertaken in which the bed length was varied. In these simulations, the solid temperature increased sharply in the early stage of drying, and then approached to a temperature nearly the same as the drying air temperature, and finally, the solid temperature remained nearly constant until the dryer exit. Similar profiles were obtained by Verma and Paliwal (2022). Additionally, Khanali *et al.* (2013) reported a similar experimentally behaviour for rough rice drying in a plug-flow fluidised bed dryer and then confirmed by Picado and Gamero (2014) employing simulations.

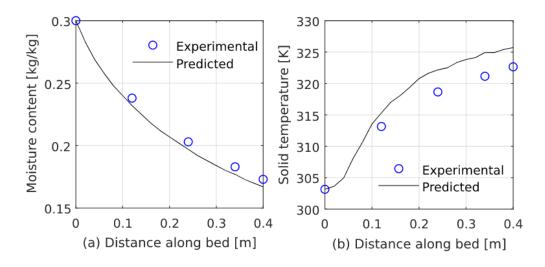


Fig. 4 Comparison between experimental and predicted moisture content along the bed length. $T_{g,0} = 323.15 \text{ K}, Y_0 = 0.0215 \text{ kg/kg}, X_0 = 0.30 \text{ kg/kg}, T_{s,0} = 303.15 \text{ K}$

3.2 Parametric studies

Because knowledge of the parameters that significantly impact drying behaviour is useful in designing dryers, simulations were extended to predict the effects of operating parameters. The basic data used in the simulations that follow were the same as those in Fig. 4. In all cases, a \pm 15% variation in the operating parameters was applied. Figure 5 depicts the effect of inlet gas temperature on the moisture content profile along the length of the dryer. As expected, the evaporation (drying) rate increases with the inlet gas temperature, thus resulting in lowering solid moisture content. This effect can be attributed to the controlling rate of water vapour transfer inside the grain due to moisture diffusion towards the surface.

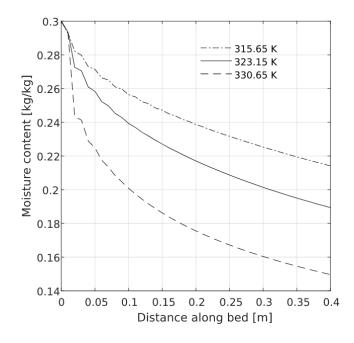


Fig. 5 Effect of gas temperature on drying behaviour. $u_g = 3 \text{ m/s}$, $Y_0 = 0.0215 \text{ kg/kg}$, $X_0 = 0.30 \text{ kg/kg}$, $T_{s,0} = 303.15 \text{ K}$, S = 0.50 kg/min.

Figure 6 illustrates the effect of particle diameter on the moisture content profile along the length of the dryer. As shown in Fig. 6, increasing the particle diameter reduces the evaporation of the solid moisture content. Larger particles contain much longer diffusional paths within the solid, thus increasing internal resistance against mass transfer. Further, the changes in particle diameter had very little effect on the solid temperature along the length of the dryer (results not shown).

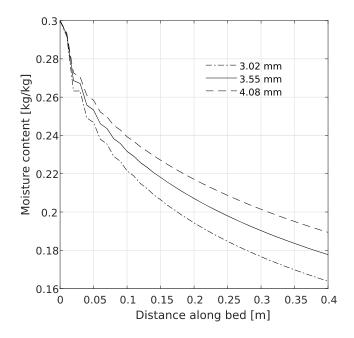


Fig. 6 Effect of particle size on drying behaviour. $u_g = 3 \text{ m/s}$, $T_{g,0} = 323.15 \text{ K}$, $Y_0 = 0.0215 \text{ kg/kg}$, $X_0 = 0.30 \text{ kg/kg}$, $T_{s,0} = 303.15 \text{ K}$, S = 0.50 kg/min.

At the conditions chosen for calculations, it was found that changes in gas velocity, dry solid flow, and the solid temperature had essentially no effect on drying behaviour. A similar result has also been reported by Bizmark *et al.* (2010) and Khanali *et al.* (2013).

The solid moisture contents decrease non-linearly along the length of the dryer as shown in Figs. 5 and 6. Similar results were reported by Khanali *et al.* (2013), Alonso and Picado (2021), and Nilsson (1986) for rough rice, shelled corn, and apatite granules, respectively. However, a linear decreasing moisture content profile along the length of a continuous plug-flow fluidised bed dryer was also reported in the literature (Izadifar and Mowla, 2003).

4. CONCLUSIONS

In this study, a continuous plug-flow fluidised bed dryer model has been employed. The predicted moisture content using the proposed model showed a very good agreement with experimental data. Simulations based on this model were conducted to study the effects of operating parameters, such as gas temperature, gas velocity, particle size, dry solids flow and inlet solid temperature on the moisture content. An increase in gas temperature induces faster drying. As the particle diameter was increased, the drying process slowed down. In these calculations, gas velocity, dry solids flow, and the solid temperature had essentially no effect on the drying process. The present model could be a useful tool for process exploration and optimisation of this type of dryer.

ACKNOWLEDGEMENTS

The authors gratefully acknowledge the financial support provided by the Swedish International Development Cooperation Agency (Sida). A. Picado also acknowledges Panabits, Panama for providing the digitalisation of the experimental data.

CONFLICT OF INTEREST

The authors declare that there is no conflict of interest regarding the publication of this article.

NOTATION

| a_s | Specific area per unit bed volume | $(m^2 m^{-3})$ |
|---------|--|----------------------------|
| B | Dryer width | (m) |
| D | Mass transport coefficient | $(m^2 s^{-1})$ |
| D_h | Thermal diffusivity | $(m^2 s^{-1})$ |
| F | Mass flow per cross-section, dry basis | $(kg m^{-2} s^{-1})$ |
| G_{g} | Molar evaporation flux | $(kmol m^{-2} s^{-1})$ |
| h | Heat transfer coefficient | $(W m^{-2} K^{-1})$ |
| H_b | Bed height | (m) |
| I | Enthalpy per unit mass, dry basis | $(J kg^{-1})$ |
| k | Thermal conductivity | $(W m^{-1} K^{-1})$ |
| L | Dryer length | (m) |
| M | Molecular weight of the moisture | (kg kmol ⁻¹) |
| q | Heat flux | $(J m^{-2} s^{-1})$ |
| r | Radial coordinate | (m) |
| S | Flow of dry solids | $(kg s^{-1})$ |
| t | Time | (s) |
| T | Temperature | (K) |
| u_g | Gas velocity | $(m s^{-1})$ |
| V | Flow of dry gas | $(kg s^{-1})$ |
| v | Forward bed velocity | $(m s^{-1})$ |
| X | Solid moisture content, dry basis | $(kg kg^{-1})$ |
| у | Molar fraction in the gas phase | (kmol kmol ⁻¹) |
| Y | Gas humidity, dry basis | $(kg kg^{-1})$ |
| Z | Distance along the length of the bed | (m) |
| | | |

Greek Letters

| δ | Particle radius | (m) |
|---------------|-----------------------------|-------------------------|
| \mathcal{E} | Porosity | (-) |
| λ | Latent heat of vaporisation | (J kmol ⁻¹) |
| ρ | Density | $(kg m^{-3})$ |

Subscripts

| b | Bed | S | Solid |
|-----|-----------------|----------|-----------|
| e | Exit | t | Total |
| eff | Effective value | δ | Interface |
| g | Gas | ∞ | Gas bulk |
| p | Particle | 0 | Inlet |

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